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Design of a Backstepping-Controlled Boost Converter for MPPT in PV Chains

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*Abstract***—The objective of this work is to integrate the backstepping control for tracking the maximum power point of a photovoltaic (PV) chain. This control strategy is applied for a parallel DC-DC converter (type: boost) in order to regulate the output voltage of the PV generator, according to the reference voltage generated by the known perturb and observe (P&O) MPPT (maximum power point tracking) algorithm. The robust and nonlinear backstepping controller is based on Lyapunov function for ensuring the local stability of the system. The basic idea of the nonlinear backstepping controller** *(BSC***) is to synthesize a control law in a recursive way, that is to say step by step. This controller has a good transition response, a low tracking error, and a very fast response to the changes in solar irradiation and environmental temperature. To prove the effectiveness of the suggested control method, a comparative study through numerical simulations is presented with sliding mode control (***SMC***) and the classical** *PI* **(proportional-integral) controller.**

Keywords— Boost converter; backstepping control; robustnes maximum power point tracking (MPPT); photovoltaic chain

I. INTRODUCTION

In recent years, a very important development of renewable energies has occurred because they have many advantages when compared to fossil fuels. With its inexhaustible potential and no negative impact on the environment [1], renewable energy is an appropriate and accessible technology for economic growth and sustainable development [2]. The study of the renewable energy conversion chain: primary energy extraction, electrical conversion, power generation, network transformation, and integration, is a basic element to improve the quality of production of "green" energy.

Given the current interest of the world in renewable energy in general and solar energy especially, photovoltaic (PV) panels are used today in plenty of applications. The PV array has a single operating point that can supply maximum power to the load. This point is named the maximum power point (MPP). The locus of this point has a nonlinear variation with temperature and solar radiation. Thus, in order to work the PV array at the MPP, the PV chain must include a maximum power point tracking (MPPT controller)

The boost type DC-DC converter is used generally in the PV chain as adaptation stage [3, 4]. This latter is connected to the output of the PV array and controlled by MPPT (Maximum power point tracking) algorithm in order to achieve the optimal voltage or current for harnessing the maximum PV energy.

Numerous MPPT methods have been developed and documented in the literature such as perturb and observe (P&O) [5-7], incremental conductance [2, 7-8], predictivemodel-based approaches [9-11], sliding mode control-based MPPT (*SMC*) [12-15], fuzzy and artificial neural network methods [16-18].

In this paper, a robust nonlinear backstepping controller, which controls the duty cycle of a boost converter, is suggested. The output voltage of the PV array is the variable to be controlled; the output reference voltage of the PV array is delivered by a P&O algorithm to reach the MPP speedily. Consequently, the robustness is increased and Lyapunov's law ensures the global asymptotic stability and MPP is achieved even any environmental conditions.

This paper is structured as follows: in the second section description of PV chain, PV panel and boost k; modeling are introduced. In the third section, the backstepping control is detailed. Section *IV and V,* depict respectively analysis of the simulation results and comparison with SMC and *PI* controller and finally the conclusion.

II. DESCRIPTION OF PHOTOVOLTAIC CHAIN

The configuration of the PV chain under studied is given in Fig. 1. It represents a stand-alone structure composed of:

Fig. 1. Photovoltaic chain

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- PV array which produces electrical energy directly from solar radiation.
- DC-DC boost converter with resistive load controlled by backstepping controller to release the MPPT operation. The backstepping controller block is the most important part of the system because it guarantees the necessary energy to the load.

A. PV panel modeling

The PV panel considered in this work is *SIEMENS SM 110-24*, which is simulated using the model proposed in [18]. This model comprises a current generator in parallel with, series and shunt resistances *Rs* and *Rsh* Respectively.

The equations below are used to calculate the current generated by the PV panel :

$$
I_{PV} = I_{Ph} - I_0 \left[exp\left(\frac{V_{PV} + Rs.I_{PV}}{\alpha.Vt}\right) - 1\right] - \left(\frac{V_{PV} + Rs.I_{PV}}{R_{Sh}}\right) (1)
$$

$$
I_{Ph} = \left(I_{PV_{-n}} + Ki\Delta T\right)\frac{G}{G_n} \tag{2}
$$

$$
Vt = \frac{Ns.K.T}{q}
$$
 (3)

$$
I_0 = \frac{I_{sc_n} + K.\Delta T}{\exp(V_{oc_n} + \frac{Kv.\Delta T}{\alpha.Vt})}
$$
(4)

with

 $\Delta T = T - Tn$ (*T* and *Tn* are the actual and nominal temperature respectively). $I_{PV,n}$ and G_n are respectively the current generated by the light and the solar irradiation under nominal conditions. *Ki* and *Kv* are the current and voltage coefficients respectively. $V_{oc,n}$ and $I_{sc,n}$ are respectively the open circuit voltage and short-circuit current of the panel at nominal temperature. I_0 is the dark saturation current. I_{ph} is the photogenerated current. V_t is the thermal voltage. Rs and Rsh are series and shunt resistances respectively. *Ns* is the number of series cells in a PV panel and α is the diode quality factor. *K* is Boltzmann's constant and *q* is is electrical charge.

The PV array is comprised of several PV panels connected in series and parallel. Therefore, regarding on the PV panel model given by the Eq. 3, the PV array model can be expressed as

$$
I_{\scriptscriptstyle{pv}} = N_{\scriptscriptstyle{pv}}. I_{\scriptscriptstyle{p_{\scriptscriptstyle{0}}}} - N_{\scriptscriptstyle{pv}}. I_{\scriptscriptstyle{0}} \left[exp\left(\frac{N_{\scriptscriptstyle{u}}, V_{\scriptscriptstyle{pv}} + Rs. I_{\scriptscriptstyle{w}} \left(\frac{N_{\scriptscriptstyle{u}}}{N_{\scriptscriptstyle{p}}}\right)}{ \alpha.Vt.N_{\scriptscriptstyle{u}}} \right) - 1 \right] - \left(\frac{N_{\scriptscriptstyle{u}}, V_{\scriptscriptstyle{pv}} + Rs. I_{\scriptscriptstyle{pv}} \left(\frac{N_{\scriptscriptstyle{u}}}{N_{\scriptscriptstyle{p}}}\right)}{R_{\scriptscriptstyle{0}} \left(\frac{N_{\scriptscriptstyle{u}}}{N_{\scriptscriptstyle{p}}}\right)} \right) \right]
$$

where *Npp* and *Nss* are the numbers of *PV* panels that are connected in parallel and series respectively.

B. Boost chopper modeling

The Dc-Dc boost converter is applied to step-up a DC voltage [3, 13]. This latter is used to shift the PV output voltage (*VPV*) to the desired *Vmpp* by changing the value of duty cycle. The principal electrical circuit diagram of the boost chopper is presented in Fig. 2. It consists of the main components: Input voltage (*VPV*), Transistor switches (*S*), Inductor (*L*), Diodes (*D1 & D2*), Capacitor (*C1 & C2*), Load (*R*).

Fig. 2. Boost converter

It is assumed that the boost chopper is operating in *CCM* (the current *IL* crossing the inductance *L* never get zero). There are two operating intervals of the converter, i.e. *interval 1*, in which the switch is turned *On*, and *interval 2*, in which the switch is turned *Off*.

interval 1, for the first period μTs : the IGBT switch (S) is *ON*, the load *R* is disconnected due to the closed path by switch (*S*). Inductor (*L*) is charged from PV array through switch (*S)* in this mode

Using Kirchhoff's voltage and current law, we can write

$$
\begin{cases}\nIc_1 = C_1 \frac{dV_{PV}}{dt} = I_{PV} - I_L \\
Ic_2 = C_2 \frac{dV_0}{dt} = -I_0 \\
V_L = L \frac{dI_L}{dt} = V_{PV}\n\end{cases}
$$
\n(6)

• *Interval 2*, for the second period $(I-\mu)Ts$: the switch (S) is turned *OFF* and the load *R* is connected directly to the inductor (L) via diode $(D2)$.

Using kirchhoff's law, it yields

$$
\begin{cases}\nI_{C_1} = C_1 \frac{dV_{PV}}{dt} = I_{PV} - I_L \\
I_{C_2} = C_2 \frac{dV_0}{dt} = I_L - I_0 \\
V_L = L \frac{dI_L}{dt} = V_{PV} - V_0\n\end{cases} (7)
$$

To find a dynamic representation valid for all the period *Ts*, one generally uses the following averaging expression

$$
\frac{dx}{dt}Ts = \frac{dx}{dt_{\mu Ts}} \mu Ts + \frac{dx}{dt_{(1-\mu)Ts}} (1-\mu)Ts
$$
 (8)

Applying the relation of Eq. 8 to the systems of Eqs. 6 and 7, we get the average model of the boost converter

$$
\begin{cases}\n\frac{dV_{PV}}{dt} = \frac{I_{PV}}{C_1} - \frac{I_L}{C_1} \\
\frac{dV_0}{dt} = (1 - \mu) \frac{I_L}{C_2} - \frac{I_0}{C_2} \\
\frac{dI_L}{dt} = \frac{V_{PV}}{L} - (1 - \mu) \frac{V_0}{L} \\
\dot{x}_1 = \frac{I_{PV}}{C_1} - \frac{x_2}{C_1} \\
\dot{x}_2 = \frac{x_1}{L} - (1 - \mu) \frac{V_0}{L}\n\end{cases}
$$
\n(10)

where $x = [x_1 \ x_2]^T = [V_{PV} \ I_L]^T$, represents the state vector and $\mu \in [0,1]$ is the duty cycles of the signal control.

III. BSC DESGIN

with a view to extracting the maximum energy from the PV array, a nonlinear controller *BSC* is aimed to track the PV array output tension V_{PV} to V_{mpp} by controlling the duty cycle μ of the boost power converter. For this reason

Step 1:

First of all, we define the error signal

$$
e_1 = V_{PV} - V_{ref} \tag{11}
$$

where V_{ref} is the voltage reference produced by the P&O algorithm. By converging the e_1 to $(e_1 = 0)$, we can acquire the desired result.

Using the Equation 10, the tracking error derivative is written as follows

$$
\dot{e}_1 = \frac{I_{PV}}{C_1} - \frac{1}{C_1} x_2 - \dot{V}_{ref}
$$
 (12)

The following Lyapunov function is considered

$$
V_1 = \frac{1}{2} e_1^2 \tag{13}
$$

In order to ensure the asymptotic stability, this function of Lyapunov must be positive $(V_1 > 1)$ definite and radially unbounded, and its derivative \dot{V}_1 with respect to time should be negative definite [19, 20]. Taking the time derivative of Eq. 13, we can get

$$
\dot{V}_1 = e_1 \dot{e}_1 \tag{14}
$$

$$
\dot{V}_1 = e_1 \left(\frac{I_{PV}}{C_1} - \frac{1}{C_1} x_2 - \dot{V}_{ref} \right)
$$
 (15)

From this latter, the derivative of Lyapunov function to be negative, it is necessary to :

$$
\frac{I_{PV}}{C_1} - \frac{1}{C_1} x_2 - \dot{V}_{ref} = -Ke_1
$$
 (16)

From where

$$
x_2 = C_1 (K_1 e_1 - \dot{V}_{ref}) + I_{PV}
$$
 (17)

Using the values of x_2 from Eq. 17, Eq. 15 becomes

$$
\dot{V}_1 = e_1 \left(\frac{I_{PV}}{C_1} - K_1 e_1 + \dot{V}_{ref} - \frac{I_{PV}}{C_1} - \dot{V}_{ref} \right)
$$
(18)

$$
\dot{V}_1 = -K_1 e_1^2 \tag{19}
$$

Since the derivative of V_I to be definitively negative, the value of K_l must be defined positively, and Eq. 14 must be satisfied.

 β : is the function of stabilization, acts as a reference current for *x2*. then defined by

$$
\beta = C_1 \left(K_1 e_1 - \dot{V}_{ref} \right) + I_{PV}
$$
\n(20)

Hence the asymptotic stability of the system given by Eq. 10 in origin.

A. Step 2:

The $2nd$ error variable (e₂), which represents the difference between the state variable x_2 and its desired value β , is defined by

$$
e_2 = x_2 - \beta \tag{21}
$$

Or

$$
x_2 = e_2 + \beta \tag{22}
$$

Differentiating Eq. 22, Eq. 12 becomes

$$
\dot{e}_1 = \frac{I_{pV}}{C_1} - \frac{1}{C_1} (e_2 + \beta) - \dot{V}_{ref}
$$
 (23)

$$
\dot{e}_1 = -K_1 e_1 - \frac{1}{C_1} e_2 \tag{24}
$$

The derivative of e_2 can define as follows

$$
\dot{e}_2 = \dot{x}_2 - \dot{\beta} \tag{25}
$$

Therefore

$$
\dot{e}_2 = \frac{1}{L}x_1 - \frac{1}{L}(1 - \mu)V_0 - \dot{\beta}
$$
 (26)

In order to ensure the global asymptotic stability of the system and the convergence of the errors e_1 and e_2 to zero, a composite Lyapunov function V_t is defined whose time derivative must be negative definite for all values of *x1* and *x2*.

$$
V_t = V_1 + \frac{1}{2}e_2^2 \tag{27}
$$

The derivative of V_t is

$$
\dot{V}_t = \dot{V}_1 + e_2 \dot{e}_2 \tag{28}
$$

$$
\dot{V}_t = -K_1 e_1^2 + e_2 \left[-\frac{1}{C_1} e_1 + \frac{1}{L} (V_{PV} - (1 - \mu) V_0) - \dot{\beta} \right] (29)
$$

For the derivative of V_t negative, it is necessary to

$$
-\frac{1}{C_1}e_1 + \frac{1}{L}(V_{PV} - (1 - \mu)V_0) - \dot{\beta} = -K_2e_2
$$
 (30)

From where

$$
\mu = 1 - \frac{1}{V_0} \left[V_{PV} - L\dot{\beta} - L \left(\frac{1}{C_1} e_1 - K_2 e_2 \right) \right]
$$
 (31)

IV. SIMULATION RESULTS

Firstly , numerical simulation of the PV chain shown in Fig. 1 is developed and implemented in MATLAB Simulink® environment. The photovoltaic array considered in this work consists of four identical PV panels shared into two parallel branches of two series connected panels. The parameters for the PV panel, the boost chopper and the *BSC* are indicated in Table 1.

TABLE I. PV MODULE , BOOST CHOPPER AND BSC CONTROLLER SPECIFICATIONS

	Parameters	Values
PV panel	Maximum power (Pmpp)	120W
	Open circuit voltage (Voc)	42.1 V
	Short circuit current (Isc)	3.87 A
	Voltage at P_{Max} (Vmpp)	33.7 V
	Current at P_{Max} (Impp)	3.56 A
	Number of cells connected in series (Ns)	72
	Number of cells connected in parallel (Np)	
	Input capacitor C1	$1100 \mu F$
Boost	Output capacitor C2	$1100 \mu F$
converter	Inductor L	1 mH
	Load _R	50 Ω
Backstepping	K_I	500
controller	K ₂	5000

A. Case 1: Test under varying levels of irradiance

Under this case, the temperature T is set constant at T= 25 °C and the irradiance \vec{G} is subjected from time to time to a gradual change and a sudden change every 0.5 sec.

 The profile of the different levels for irradiance is illustrated in Fig. 3. The profile starts at 400 W/m2 . During the first ascend $(0.5 - 1$ second), the irradiance increases gradually from 400 to1000 W/m2 .

Then, four consecutive step changes are made: (1000–600), (600–800), (800–600) and (600–1000) W/m2 . Finally, the level of irradiance descends gradually to primary state from 1000 to 400 W/m2 .

It can be seen from the results of simulations, during the variation of each irradiance level, that the proposed *BSC* tracks successfully the reference voltage *Vref* with less voltage fluctuations between (67.8- 68.2 V) has been recorded as shown in Fig. 4. The performance of the proposed controller is then confirmed.

Fig. 5 illustrated the obtained results of PV array with backstepping controller. It can be observed that the proposed controller has a very high performance at any level of irradiation and the controller performed well.

Fig. 6 shows the convergence of the error signal *e***1** to zero below the sudden variation levels of irradiance at 1.5; 2; 2.5; 3 second and the gradual variation at 0.5; 4 seconds.

B. Case 2 :Test under varying levels of temperature

In this scenario, irradiance level is set constant at $G=1000$ W/m², and temperature levels are varied.

The profile for the different levels of temperature is illustrated in Fig. 7. The profile starts at 25°C. During the first ascend $(0.5 - 1$ second), the irradiance increases gradually from 25 to 65° C.

Then, four consecutive step changes are made: (65–35), $(35-45)$, $(45-35)$ and $(35-65)$ °C. Finally, the level of temperature descends gradually from 65 to 25 °C.

From photovoltaic array curves, the performance of the *BSC* is again confirmed, and good tracking to *Vref*, as shown in Fig. 8. Thus, power P_{PV} achieves the P_{mpo} at the same time.

Moreover, one can deduce that the *BSC* presents a good transition response, and a very fast system reaction against set point change.

Fig. 10 shows the convergence of the error signal *e1* to a null value under the variation of temperature at 1.5; 2.5; 3.5 second, with a low fluctuation between $[-0.2, 0.2]$.

Fig. 3. Varying levels of irradiance

Fig. 4. Tracking of V_{PV} for different values of solar irradiation.

Fig. 5. Power of *PV* array for different values of solar irradiation.

Fig. 6. Error signal e_1 under varying irradiance.

Fig. 8. Tracking of V_{PV} for different levels of temperature

Fig. 9. Power of *PV* array for different levels of temperature .

Fig. 10. Error signal e_I under varying temperature .

V. COMPARISON WITH PI AND SMC CONTROLLER

To show the performance of the *BSC*, it is compared with *SMC* and *PI* controllers. These latter are simulated and compared with the same conditions (sampling time and PWM frequency) at varying temperature and irradiance levels.

A. Comparison under varying irradiance

Figs. 11, 12 and 9 shows respectively the simulated of PV voltage, PV power and error signal with conventional *PI* and *SMC* controllers. First of all, the irradiation level is fixed at 400 W/m². The *VPV* voltage with conventional *PI* and *SMC* methods is fluctuating around the reference *Vref* between (65.41-64.64V) and (65.53-65V) respectively.

Fig. 11. Backstepping vs **PI** and **SMC** tracking of V_{PV}

Fig. 12. Backstepping vs *PI* and *SMC* power of PV array under variation irradiance

Fig. 13. Backstepping vs *PI* and *SMC* error signal under varying irradiance.

Moreover, for the proposed *BSC*, the PV voltage tracks accurately its reference with fewer voltage fluctuations between (65.35- 65.02V).

On the other hand, it can be seen that not only the *BSC* reaches the MPP more rapidly than the PI and *SMC*, but during the variation of irradiance level at 0.5; 1.5; 2 seconds, the backstepping controller displays superior performance in terms of maximum overshoot, response time and minimal oscillations compared to the other methods.

B. Comparison under varying temperature

In this 2nd comparison test, all the regulators are tested done below varying temperature levels. The irradiance is set at 1000 W/m² and temperature firstly is stepped up gradually from T= 25 \degree C to T = 65 \degree C at 1 seconds, and suddenly stepped down and up from tow steps $T=65$ °C to 35 at 1.5 seconds and from 35 °C to 45 °C at 2 seconds.

The obtained results are illustrated in Figs. 14, 15 and 16. It can be seen that the waveforms of V_{PV} and P_{PV} are reverse proportional to the change of temperature.

The PV voltage with conventional *PI* and *SMC* methods is fluctuating around the reference *Vref* between (58.54-57.4V) and (58.53-57.42V) respectively, in other hand, it can be seen that *BSC* reaches our system in a minimal time with fewer oscillations between (58.22-57.99) as compared to *PI* and *SMC* controllers. On the same figures a zoomed view of the fluctuations about the MPP of all controllers.

Fig. 14. Backstepping vs **PI** and **SMC** Tracking of V_{PV}

Fig. 15. Bachsteppng vs *PI* and *SMC* power of PV array under variation temperature

Fig. 16. Backstepping vs *PI* and *SMC* error signal under varying temperature

VI. CONCLUSION

In this paper, robust and nonlinear backstepping has been applied to track the maximum power point MPP of a photovoltaic system .

The PV generator is to the load (resistance) via through a DC-DC boost power converter.

The PV generator is is linked to the load (resistor) via a DC-DC boost power converter. To get maximum power P_{mpp} from photovoltaic array, the duty cycle μ of the boost chopper is controlled through which the PV array output voltage is tracked to the voltage reference , this latter has been generated by the P&O method.

The verification of the asymptotic stability of photovoltaic chain is performed via Lyapunov stability analysis. The simulation results show that the controller *BSC* verified and performed well below the sudden and gradual variation of climatic conditions, which prove the good robustness of the *BSC* proposed controller.

The comparison with the traditional technic used in the past P&O/PI and SMC/PI controllers are made which shows that the *BSC* performed better and most efficiently during the variation in the climatic conditions (irradiance & temperature levels).

As a future perspective, an implementation of the proposed controller using a dSPACE system be introduced.

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